

Concurrent Lines in a Triangle

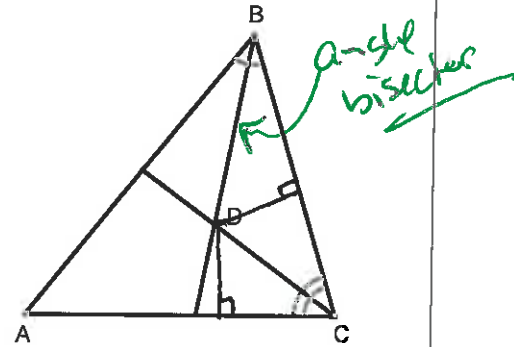
Example 1:

1. Point D can be described as:

- a) a Circumcenter b) an Orthocenter
 (c) an Incenter d) a Centroid

2. If the distance from D to $\overline{AC} = 5x - 10$ and the distance from D to $\overline{BC} = 3x + 4$, Find x.

$$\begin{aligned} 5x - 10 &= 3x + 4 \\ 2x &= 14 \\ x &= 7 \end{aligned}$$



Example 2:

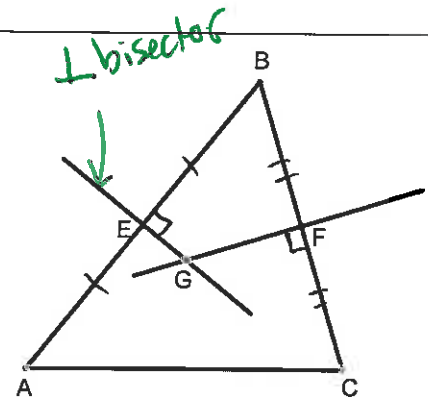
Given: $\triangle ABC$ with Circumcenter G:

1. \overline{EG} can be described as:

- a) Median b) \angle bisector c) \perp bisector d) Altitude

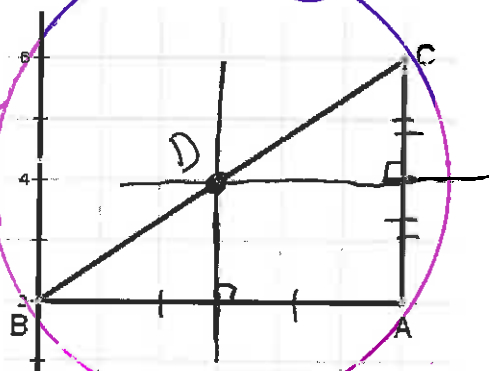
2. If $AG = 3x - 8$ and $BG = 4x - 20$, find x.

$$\begin{aligned} 3x - 8 &= 4x - 20 \\ 12 &= x \end{aligned}$$



Example 3:

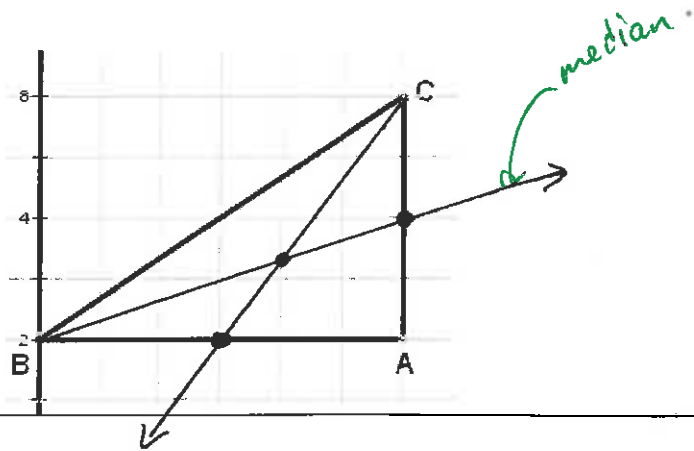
Find the center of the circle that can be circumscribed around $\triangle ABC$.



Circumcenter

Example 4:

1. Locate the Centroid of $\triangle ABC$.



Example 5:

1. Point G can be described as:

- a) Centroid b) a Circumcenter
c) an Incenter d) an Orthocenter

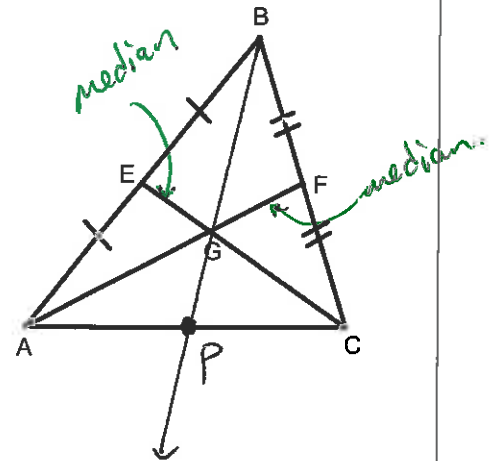
2. If the intersection of ray \overrightarrow{BG} and \overline{AC} is point P. What is the ratio of $BG:GP$?

- a) 3:1 b) 2:3 c) 2:1 d) 1:2


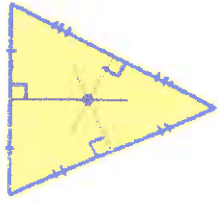
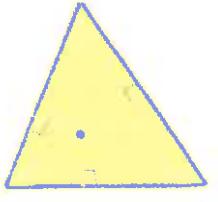
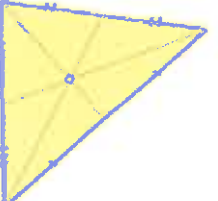
3. If $GP=18$, find BG and BP .

$$BG = 2GP$$
$$BG = 2(18) = 36$$

$$BP = BG + GP$$
$$= 18 + 36$$
$$= 54$$



Triangle Centers Summary

	Point of Concurrence	Theorem	Picture	Location
∠ Bisectors	<i>Incenter</i>	<i>equidistant to the sides.</i>		Acute: In Obtuse: In Right: In
⊥ Bisectors	<i>Circumcenter</i>	<i>equidistant to the vertices.</i>		Acute: In Obtuse: out Right: on
Altitudes	<i>Orthocenter</i>	<i>none</i>		Acute: In Obtuse: out Right: on
Medians	<i>Centroid.</i>	<i>Divides median into 2:1 ratio</i>		Acute: In Obtuse: In Right: In

